

5.7.2.2. The Traditional Display of the Minkowski space

In Figure 5.54 we display the extension in two dimensions γ_1, γ_2 (two 1-vector *directions*) as an *extension plane* $\gamma_1\gamma_2$, supported by an ordinary spacelike bivector *direction* $\gamma_1\gamma_2$, where

$$(5.332) \quad (\gamma_1\gamma_2)^2 = \gamma_1\gamma_2\gamma_1\gamma_2 = -\gamma_1\gamma_1\gamma_2\gamma_2 = -1.$$

We ‘look’ into the depth of the passed side of this extension plane of Figure 5.54 with a unit circle ring \circ symbolising the rotation symmetry around the information development *direction*.

Then we have two *directions* of the two Minkowski \mathcal{B}_k -bivector-planes

$$(5.333) \quad \mathcal{B}_1 := \gamma_1\gamma_0, \quad \mathcal{B}_2 := \gamma_2\gamma_0, \quad \text{with } \mathcal{B}_1^2 = \mathcal{B}_2^2 = 1.$$

We add these two together as a function of the circular rotation with the Euler angle argument θ

$$(5.334) \quad \mathcal{B}_\theta = \cos(\theta)\mathcal{B}_1 + \sin(\theta)\mathcal{B}_2 = \gamma_\theta\gamma_0 = (\cos(\theta)\gamma_1 + \sin(\theta)\gamma_2)\gamma_0$$

Right multiplying the last parenthesis with $-\gamma_1\gamma_1=1$ we achieve the Euler rotation

$$(5.335) \quad \mathcal{B}_\theta = \gamma_\theta\gamma_0 = (\cos\theta + \gamma_1\gamma_2\sin\theta)\gamma_1\gamma_0 = (e^{\gamma_1\gamma_2\theta})\mathcal{B}_1.$$

To intuit this, we project the subject \mathcal{B} -planes $\mathcal{B}_1, \mathcal{B}_2$, and \mathcal{B}_θ into our object plane given by $\mathbf{i} := \sigma_2\sigma_1$, using the projection mapping operation rules expressed in (5.328)

$$(5.336) \quad \sigma_1 \equiv \gamma_1\gamma_0 = \mathcal{B}_1, \quad \sigma_2 \equiv \gamma_2\gamma_0 = \mathcal{B}_2, \quad \text{and} \quad \hat{\mathbf{r}}_\theta \equiv \gamma_\theta\gamma_0 = \mathcal{B}_\theta = e^{\gamma_1\gamma_2\theta}\mathcal{B}_1 \equiv e^{i\theta}\sigma_1.$$

Now the *extension plane* supported by $\gamma_1\gamma_2$ is mapped into the Euclidean plane supported by $\mathbf{i} = \sigma_2\sigma_1 \equiv \gamma_1\gamma_2$. Here the rotation is described by the 1-rotor $\hat{\mathbf{r}}_\theta\sigma_1 = e^{i\theta}$, for $\forall\theta \in \mathbb{R}$.

Also for the \mathcal{B}_θ *direction*, we note that $\gamma_\theta^2 = -1$ is Minkowski space extension signature $(-)$.

The nilpotent isotropic signal of information from the isometric idea $|\gamma_\theta| = |\gamma_0| = 1$ when gives the *null line* balance $|\tau\gamma_\theta| = |\tau\gamma_0| = \tau \in \mathbb{R}$. This *null line* situation is rotated with $e^{\gamma_1\gamma_2\theta}$ around the development *direction* γ_0 in a so-called *null cone*. When inside this cone, information can be exchanged for future expectations called events or from passed phenomena called memory.

The development is driven by the circling oscillator $\circ = e^{\gamma_1\gamma_2\theta} \equiv e^{i\theta} = e^{i\theta\omega\tau}$, where the phase angle is $\theta = \omega\tau = \tau$ by defining the development parameter $\tau \in \mathbb{R} [\hat{\omega}^{-1}]$, setting its frequency energy $\omega = \hat{\omega} := 1[\hat{\omega}]$ as the counting clock norm. Then *null* tangent on the *null cone* seems to follow a conic spiral with expanding radius of $c|\theta\gamma_\theta| = c|\tau\gamma_\theta|$ relative to the reference $|\gamma_0|=1$. For $|\theta| > 1$ the tangent speed of the oscillator rotating *null cone* in the display will grow and exceed the speed of information $c1$. It is obvious that the extended circumference arc speed of the circle oscillator does not exceed $c1$, ($c=1$) therefore a unit circle oscillator $|\hat{\mathbf{r}}_\theta|=|\gamma_\theta|=|\gamma_0|=1$ is the binding. The plane rotation $e^{i\theta} = e^{\sigma_2\sigma_1\theta} = e^{\gamma_1\gamma_2\theta}$ initiates a third normal extension *direction* $\sigma_3 \equiv \gamma_3\gamma_0$ as an axis of rotation in 3-space.²⁷⁵ The a priori idea is, that information development isometry is isotropic distributed over all extended *directions* in 3-space, whence we judge

$$(5.337) \quad |\gamma_\theta| = |\gamma_1| = |\gamma_2| = |\gamma_3| = |\gamma_0| = 1.$$

From this isotropic isometry, we have ambiguity in what space extension *direction* to intuit for *one quantum* of information as a unit *direction* \mathcal{B} -bivector. The information isometry can only follow one nilpotent pair *null lines direction* $\mathcal{B} = n\wedge\bar{n}$ inside its Minkowski \mathcal{B} -plane *direction*. One intuit picture is the oscillation rotation of the information \mathcal{B}_θ -plane has one persistent oscillating 1-vector extension *direction* γ_θ always orthogonal to the future-oriented development *direction* γ_0 principal isotropic in all spatial *directions* a priori orthogonal to all these extensions $\forall\gamma_\theta \cdot \gamma_0 = 0$, it can be perpendicular to some extensions $\gamma_0 \perp \gamma_\theta$ and parallel to one other *direction*, e.g. $\gamma_0 \parallel \gamma_3$, but still always orthonormal $\gamma_0 \cdot \gamma_k = 0$ and $|\gamma_\mu| = 1$, $\mu = 0,1,2,3$, as .

Actively γ_0 can be parallel with one straight line extension *direction* e.g., $\sigma_3 \equiv \gamma_3\gamma_0$, $\gamma_3 \cdot \gamma_0 = 0$ and ambiguously simultaneous be curved²⁷⁶ along the circumference arc of the oscillating unit circle radius $|\hat{\mathbf{r}}_\theta| = |\gamma_\theta|=1$ so that $\gamma_0 \perp \gamma_\theta$ and substantial $\gamma_0 \cdot \gamma_\theta = 0$, (see below Figure 5.55).

²⁷⁵ In chapter 6 we will look further into the structure of the three-dimensional natural 3-space

²⁷⁶ The ideology of a tangent vector is not necessary strait. Straitens of a non-extensive development γ_0 *direction* has no meaning.

Only one *direction* in the form of a \mathcal{B}_θ -plane can participate in the propagation of *one quantum* of active information at a time. This *quantum direction* is the nilpotent unit (5.312) $\mathcal{B}_\theta = n\wedge\bar{n}$. To possess the *quality* of autonomous extension for an *entity* it has to give its own measure in form of an oscillator giving the a priori count of development. The frequency energy of this oscillator we use as the norm i.e., $|\omega|=1$. The *direction* of oscillation we describe by the Euclidean plane bivector $\gamma_1\gamma_2 \equiv \sigma_2\sigma_1 = \mathbf{i}$. The *direction* of development γ_0 is orthonormal to both γ_1 and γ_2 expressed by (5.303). The bivector idea $(\gamma_1\gamma_2)$ is also orthogonal to γ_0 in that the inner product

$$(5.338) \quad \gamma_0 \cdot (\gamma_1\gamma_2) = \frac{1}{2}(\gamma_0\gamma_1\gamma_2 - \gamma_1\gamma_2\gamma_0) = 0.²⁷⁷$$

Hereby we decide on a shortcut and promote the subject idea $(\gamma_1\gamma_2)$ to the object $\sigma_2\sigma_1 = \mathbf{i}$

$$(5.339) \quad \gamma_1\gamma_2 = \sigma_2\sigma_1 = \mathbf{i} = \mathbf{i}_3$$

and name \mathbf{i}_3 for the plane bivector seen from a third extension direction (see below Figure 5.55). The plane circle oscillator for the autonomous isometric measure is short

$$(5.340) \quad \circ = e^{\gamma_1\gamma_2\theta} = e^{i\theta} = e^{i_3\theta}.$$

This circular oscillating 1-rotor of form $e^{i\theta}$ for the Euclidean plane leaves all the multivectors we have treated above invariant, but of course, changes their *directions*. Special the \mathcal{B}_θ -bivector *direction* is rotated in this oscillation. Inside this \mathcal{B}_θ -plane the nilpotent *null directions* n and \bar{n} is invariant preserved also by the hyperbola transformation (5.322).

²⁷⁷ Here we use the mixed grade rule (6.43) below.

When it comes to the wedge part $\gamma_0 \cdot (\gamma_1\gamma_2) = \frac{1}{2}(\gamma_0\gamma_1\gamma_2 - \gamma_1\gamma_2\gamma_0) = \gamma_1\gamma_2\gamma_0 = i\gamma_3$ we get a 3-vector as later below III. (7.15), where this three-vector concept is dual to the 1-vector idea γ_3 by the *grade-4* pseudoscalar i of STA.