

3.6. The Cyclic Quantum Oscillator Idea

We are now looking at an frequency-energy active *entity* Ψ as a single unified *entity* in physics. We assume that Ψ can be split into a *spectrum* of cyclic oscillators Ψ_ω given by circle rotations as a *primary quality*.

We remember that every circle oscillator *entity* Ψ_ω is given by an angular frequency energy *quantity* $\omega \in \mathbb{R}$ is defined as a continuous *spectrum*, as a prerequisite for Fourier transformations (1.81) section 1.7.7 and later below II. 4.1.4.2.

The stat-mode for a circle oscillator which we now call ψ_ω are mutually orthogonal when $\omega \neq \omega'$ as shown by (1.88). We remember that $\omega \in \mathbb{R}$ can be both positive and negative, as we defined it in section 3.1.7 of the cyclical rotation, which naturally applies to a harmonic circle oscillator

rotation	$u_\omega = e^{-i\omega t}$	$u_\omega^* = e^{+i\omega t}$	
$\omega > 0$	retrograde – clockwise	progressive - contra-clock	$\curvearrowright \curvearrowleft$
$\omega < 0$	progressive – contra-clock	retrograde - clockwise	$b \ d$ $p \ q$

Table 3.1 In the physics of a transversal plane of a circle rotation there is only one double degradation. The progressive is represented by $(+i, \omega > 0)$ or $(-i, \omega < 0)$ and the retrograde is represented by $(-i, \omega > 0)$ or by $(+i, \omega < 0)$.

The fundamental ideological foundation of the frequency image is the cyclic oscillation in a circle rotation where the *angular-frequency-energy* and *angular momentum* apply the quantum mechanical eigenvalue equations

$$(3.283) \quad \hbar\omega(a_+^\dagger a_+ + a_-^\dagger a_- + 1)\psi(\varphi) = E_\omega\psi(\varphi) \quad \text{and} \quad \hbar(a_+^\dagger a_+ - a_-^\dagger a_-)\psi(\varphi) = \vec{L}_3\psi(\varphi).$$

I have above advocated, that these operators act on the virtual state modes $\psi(\varphi)$. States that not only oscillate in a transversal plane but also propagates into the future space, which is orthogonal to the oscillation plane. I.e., they produce a space of the past. (see e.g., -13)

The idea of the angular momentum operator $\hat{L}_3 = \hbar(a_+^\dagger a_+ - a_-^\dagger a_-)$ tests the virtual state-mode $\psi(\varphi)$ for rotation in a transversal plane \odot to a *direction* \mathbf{e}_3 , where $\odot \perp \mathbf{e}_3$ in space.

We have seen that the transversal circular rotation assumes eigenvalues $|\vec{L}_3| = \hbar 1$ with two states of angular momentum $\vec{L}_3 = \pm \hbar \vec{1} \parallel \mathbf{e}_3$,¹⁴⁹ with the sign + for progressive $\vec{L}_3^+ = +\vec{1}$, and - for retrograde $\vec{L}_3^- = -\vec{1}$ rotation helicity, if $\hbar = 1$.

The idea of the Hamilton operator $\hat{H} = \hbar\omega(a_+^\dagger a_+ + a_-^\dagger a_- + 1)$ tests the virtual state mode $\psi(\varphi)$ condition of the angular frequency energy ω by first annihilating both the positive and the negative helicity, and then creating them identic again based on the idea of angular frequency energy *quantity* ω per se (itself).

Such an *entity* Ψ_ω , that satisfies (3.283) not only represents the concept of angular frequency energy of oscillation but also defines the concept of a *direction* $\hat{\omega}$ caused by the angular momentum $\hat{\omega} = \vec{L}_3^+ = -\vec{L}_3^- = \hbar \vec{1}$. The main contention is that this is the *direction* from the past into the future, *FORWARD* through a transversal plane $\odot \perp \hat{\omega} \parallel \mathbf{e}_3$.

This creates a quantum mechanical phase angle of development $\varphi = \omega t + \theta$, parameterised by t . The fundamental physical *entity* for one quantity called a *subton* and the *spectrum* $\vec{\omega}$ is written

$$(3.284) \quad \Psi_{\vec{\omega}}(\varphi) \sim \psi_{\pm \vec{\omega} \perp \odot}(t) = 2 \frac{1}{\sqrt{\pi}} \rho e^{-\frac{1}{2}\rho^2} \odot(e^{\pm i\omega t})_{\odot \perp \vec{\omega}}, \quad \text{for } \forall \vec{\omega}, \quad \omega = |\vec{\omega}| \in \mathbb{R}_+.$$

These angular frequencies $\omega [\hat{\omega}]$ should be counted as a *quantity* for us, it must be related to a given external angular frequency reference $\hat{\omega} \equiv 1 [\hat{\omega}]$. (Ding für Uns). The *quality* is the *direction*.

¹⁴⁹ The idea $|\vec{1}| = 1$ is the auto-norm of the quantum circle oscillator and not directly linked to our external norm $|\mathbf{e}_3| = 1$. It is the idea that the *direction* is the same $\mathbf{e}_3 \parallel \vec{1}$ (for autonomous *subton*, as for the condition a *direction* for us).

3.6.1.2. The Direction

The *direction* in space, as a *primary quality* of an object for the development, is here indicated as a unit vector $\mathbf{e}_3 = \hat{\omega}$, given by $|\mathbf{e}_3| = |\hat{\omega}| \equiv \hat{\omega} \equiv 1$, due to the reference for the frequency norm $\hat{\omega} \equiv 1 [\hat{\omega}]$, and the fact $|\hat{\omega}^{-1}| = |\hat{\omega}|$ under condition $c=1$. Then we can write the rotation vector for an angular frequency ω as $\vec{\omega} = \omega \hat{\omega} = \omega \hat{\omega} \mathbf{e}_3 = \omega \mathbf{e}_3 [\hat{\omega}]$. Does the vector $\vec{\omega}$ have a *direction* with a negative orientation $\omega < 0$, it simply represents the retrograde helicity.

The sign $\pm i$ in (3.284) for helicity ± 1 may be omitted when we let the negative frequencies represent retrograde helicity. But on the other hand, it is practically advantageous to use $\pm i$ for the helicity when the double degeneration at the same frequency $|\omega|$ are combined in a superposition. Therefore $e^{-i\omega t}$ and $e^{+i\omega t}$, are the normal way of writing the two helicities. This implies full coverage for *entities* $\Psi_{\omega \pm}$ by using only positive frequencies $\omega > 0$.

We just complement the angular momentum *quantum* numbers for the helicity ± 1 .

The *primary quality*, the *direction* is externally given by the unit vector $\mathbf{e}_3 = \hat{\omega}$, then $\vec{\omega} = \omega \mathbf{e}_3 [\hat{\omega}]$.

The *direction FORWARD* from the past into the future is given internally for the *subton* as the auto-norm *direction* $\hat{\omega}$. This internal *direction* is, of course, by its nature¹⁵⁰ parallel to the external *direction* $\mathbf{e}_3 \parallel \vec{1} = \hat{\omega}$. Auto normalization means that the frequency refers to itself, therefore we automatically have $\hat{\omega} = \vec{1}$. This autonomous vector represents not only the *direction*, but also the angular momentum *quantum* with two orientations

$$\vec{L}_3^+ = -\vec{L}_3^- = \hat{\omega} = \vec{1}, \quad (\hbar=1), \quad \text{and the propulsive momentum } \mathbf{k}_3 = \frac{\hbar}{c} \omega \mathbf{e}_3 [\hat{\omega}],$$

and the flowing energy $\hbar\omega \mathbf{e}_3 [\hat{\omega}]$, of this relativistic¹⁵¹ *quantum one subton*, as in (3.284).

The state mode ${}^{AB}\Psi_{\vec{\omega}}(\varphi)$ of Figure 3.13 is just the transport of angular frequency energy $\omega_A = \omega_B$ along with the advancement of the development parameter $t_A = t_B$, the quantum phase angle is propagated and preserved $\phi_A = \phi_B = \omega_A t_A = \omega_B t_B$. The picture is that a *subton* as a carrier ω_c *FORWARD* propagating a chronometer time $\{t_c\}$, and creates a past t_3 , that with the speed of light becomes the extension (3.265)

$$|x_3| = c |{}^{AB}\phi_c| / |\omega_c| = c |t_{c,B} + t_3| - c |t_{c,A}| = c |t_3| \quad [c\hat{\omega}^{-1}]$$

The past times with the speed of light are precise, which corresponds to spatial migration. The extension of this has a *direction* expressed as $\vec{x}_3 = x_3 \mathbf{e}_3 [c\hat{\omega}^{-1}]$.

We have here to be aware of the ambiguity of our vector \mathbf{e}_3 for the *direction* in space, as a *primary quality of first grade*:

- for the extension x_3 dimension we have a unit vector $\mathbf{e}_3 [c\hat{\omega}^{-1}]$, and
- for angular frequency energy ω propagating state-mode dimension as a unit vector $\hat{\omega} = \mathbf{e}_3 [\hat{\omega}]$.

The *direction* is one and the same in natural space in physics, and the ambiguity problem disappears in math when $\hat{\omega} = \hat{\omega}^{-1} = 1 = c$, and $\hbar=1$ for energy/frequency =1, but it is in the ethical intuition important to distinguish an a priori foundation of physics.

¹⁵⁰ This is something we determine in our autonomous intuition of the whole concept for the *subton* idea. (An synthetic judgment).

¹⁵¹ We recall here for *subtons* there is no portable energy, which is expressed by the Lagrange function $L_\omega = T_\omega - V_\omega = 0$. We call it light like as propagating energy, that only consists of state-mode energy for *subtons* which ontological have the speed of light.