

# Research on the a priori of Physics

*Geometric Critique of  
Pure Mathematical Reasoning.*

by

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*Geometric Critique of Pure Mathematical Reasoning*

Jens Erfurt Andresen  
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# Research on the a priori of Physics

## Geometric Critique of Pure Mathematical Reasoning

### Edition 2, © 2020-22

#### Jens Erfurt Andresen

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